# MENTAL MODELS FOR TRADING 

KALID AZAD, BETTEREXPLAINED.COM

## 1

"Negative numbers darken the very whole doctrines of the equations..."

- FRANCIS MASÈRES, 1759


## WHY WAS THAT HARD?

## Chap.LXVI. Of Negative Squares.

Yer is not that Suppofition (of Negative Quantities, ) either Unufeful or Abfird; when rightiy underfond. And though, as to the bare Algebraick Notation, it import a Quantity lefs than nothing: Yet, when in comes to a Phy. fical Application, it denotes as Real a Quantity as if the Siga werse-f; but to be interpreted in a contrary fenfe.

As for inftance: Suppofing a man to have advanced or moved forward, (from A to B,) 5 Yards; and then to retreat (from B to C) 2 Yards: If it be asked, how much he had Advanced (upon the whole march) when at C ? or how many Yards he is now Forwarder than when he was at A? I find (by Sulducting 3 from 5, that he is Advanced 3 Yards. (Becaule $+5-2=+3$.)


But if, having Advanced ; Yards to $B$, he thence Retreat 8 Yards to $D$; and it be then asked, How much he is Advanced when at $D$, or how much Forwarder than when he was at A: I fay - 3 Yards. (Becaufe $+5-8=\ldots 3$.) That is to fay, he is advanced 3 Yards lefs than nothing.
Which in propricty of Speech, cannot be, (fince there cannot be lefs than nothing.) And therefore as to the Line A B Forward, the cafe is Impoffible.

## WALLIS, TREATISE OF ALGEBRA (1685)



MODERN DAY


## Baseline vs. Progressive



WHAT WILL WE REMEMBER?

## ADEPT Method

$$
\begin{array}{|c|c}
\text { ANALOGY } & \text { Tell me what it's like } \\
\hline \text { DIAGRAM } & \text { Help me visualize it } \\
\hline \text { EXAMPLE } & \text { Allow me to experience it }
\end{array}
$$

PLAIN ENGLISH
Describe it with everyday words

TECHNICAL
Discuss the formal details

MARKETPLACES

- Amazon
- Ebay
- Zillow


## PRICING MODELS



## FEATURE REQUESTS



EBAY

| ${ }_{\text {chem }}^{\text {sma }}$ | aipods pro |
| :---: | :---: |
|  |  |
|  |  |
| ${ }^{11}$ Call frome |  |
|  | - Applo Atirods Prowith Magsato |
| mges |  |
| Mateses | \$165.99 |
|  | come |
|  |  |
|  |  |

STANDING, UNIFIED BID

## PUBLIC MARKET

## Market Model


Public Bids

| Bid |  |  | Ask |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MM Name | Price | Size | MM Name | Price | Size |
| BATS | 204.91 | 19 - | BATS | 204.92 | 15 |
| BYX | 204.91 | 1 | BYX | 204.92 | 2 |
| DRCTEDGE | 204.91 | 12 | DRCTEDGE | 204.92 | 6 |
| EDGEA | 204.91 | 2 | EDGEA | 204.92 | 2 |
| NSDQ | 204.91 | 1 | NSDQ | 204.92 | 1 |
| NSDQ | 204.90 | 10 | NSDQ | 204.93 | 11 |
| NSDQ | 204.89 | 29 | NSDQ | 204.94 | 46 |
| NSDQ | 204.88 | 69 | NSDQ | 204.95 | 12 |
| NSDQ | 204.87 | 32 | NSDQ | 204.96 | 95 |
| NSDQ | 204.86 | 68 - | NSDQ | 204.97 | 33 - |

## CENTRAL LOCATION

TRANSPARENT INVENTORY
PRICE HISTORY
"NAME YOUR PRICE" LIMIT ORDERS "BUY IT NOW" MARKET ORDER

## GUTCHECKS

- Why does the price change?
- How many prices are there?
- Quantity of buyers/sellers vs. aggression?

| Stock Market: <br> Better Store | (ORDER BOOK \& HISTORY) |  |
| :---: | :---: | :---: |
|  |  |  |
| Central location for buyers and sellers to trade, with public prices, orders, and history | Spreads <br> Dealers Market Makers Exchanges Order Routing |  |

## OPTIONS

- Right to buy or sell at a given price, for some time
- Everyday examples
- Pre-orders
- Coupons
- Insurance
- Paid warranty


## OPTIONS

1D 5D 1M 6M YTD 1Y 5Y Max

## OPTIONS MARKET AT MANY PRICES/DATES

1 DOM

## OPTION MARKET AT DATE

May Jun Jul Aug Sep Oct Nov Dec Jan Feb Mar Apr May Jun Jul Aug Sep Nov Dec Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
 $500.008949894989498949894989498949894989498949894989498949894989498949894989498949894989498949894989498949894989498949894989498949 \quad 21.80 \%$ $495.00844984498449844984498449844984498449844984498449844984498449844984498449844984498449844984498449844984498449844984498449844920 .58 \%$ $490.007949794979497949794979497949794979497949794979497949794979497949794979497949794979497949794979497949794979497949794979497949 \quad 19.36 \%$ $485.007449744974497449744974497449744974497449744974497449744974497449744974497449744974497449744974497449744974497449744974497449 \quad 18.15 \%$ $480.00694969496949694969496949694969496949694969496949694969496949694969496949694969496949694969496949694969496949694969496949694916 .93 \%$ $475.006449644964496449644964496449644964496449644964496449644964496449644964496449644964496449644964496449644964496449644964496449 \quad 15.71 \%$ $470.005949594959495949594959495949594959495949594959495949594959495949594959495949594959495949594959495949594959495949594959495949 \quad 14.49 \%$ $465.00544954495449544954495449544954495449544954495449544954495449544954495449544954495449544954495449544954495449544954495449544913 .27 \%$ $460.004949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949494949 \quad 12.06 \%$ $455.004449444944494449444944494449444944494449444944494449444944494449444944494449444944494449444944494449444944494449444944494449 \quad 10.84 \%$ $450.003949394939493949394939493949394939493949394939493949394939493949394939493949394939493949394939493949394939493949394939493949 \quad 9.62 \%$ $445.003449344934493449344934493449344934493449344934493449344934493449344934493449344934493449344934493449344934493449344934493449 \quad 8.40 \%$ 440 .00 29492949294929492949294929492949294929492949294929492949294929492949294929492949294929492949294929492949294929492949 $435.002449244924492449244924492449244924492449244924492449244924492449244924492449244924492449244924492449244924492449244924492449 \quad 5.97 \%$ $430.001949194919491949194919491949194919491949194919491949194919491949194919491949194919491949194919491949194919491949194919491949 \quad 4.75 \%$ $425.001449144914491449144914491449144914491449144914491449144914491449144914491449144914491449144914491449144914491449144914491449 \quad 3.53 \%$
 $415.00449449449449449449449449449449449449449449449449449449449449449449449449449449449449449449449 \quad 1.09 \%$
 405.00

 390.00 - 2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051-2051
 380.00 $-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-3051-7.43 \%$ $375.00-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-3551-8.65 \%$

 360.00-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051 -5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-5051-12.30\%

## LONG STOCK

## OWN ALL PROFITS / LOSSES FOR ALL TIME

SPY $\begin{array}{lllllllllllllllllllllllllllllllllllllll} & 10 & 11 & 12 & 13 & 14 & 15 & 16 & 17 & 18 & 19 & 20 & 21 & 22 & 23 & 24 & 25 & 26 & 27 & 28 & 29 & 30 & 31 & 1 & 2 & 3 & 4 & 5 & 6 & \text { Exp } & +/-\%\end{array}$ $500.0023442345234723492350235123532354235523562356235723582358235823592359235923592360236023602360236023602361236123612361236121 .81 \%$ $495.0023372339234123442346234823492351235223542355235623572357235823582359235923592360236023602360236023602361236123612361236120 .59 \%$ $490.00232723302333233623392342234423462348235023522353235523562357235823582359235923592360236023602360236023612361236123612361 \quad$ 19.37\% $485.00231223172321232523292332233623392342234523472350235223532355235623572358235923592360236023602360236023612361236123612361 \quad 18.15 \%$ $480.0022922298230323092314231923232328233223362339234323462349235123532355235623582359235923602360236023602361236123612361236116 .93 \%$ $475.0022642272227922852292229923052311231723222327233223362341234423482351235323552357235823592360236023602361236123612361236115 .72 \%$ $470.00222722362244225322612270227822862293230123082315232123272333233823432347235123542356235823592360236023612361236123612361 \quad$ 14.50\% $465.00217621872198220922192230224022502260227022792288229723062314232123292335234123462351235423572359236023602361236123612361 \quad 13.28 \%$ 460.00211021232136214921622174218722002212222522372249226122722283229423052315232423324340234623522356235923602361236123612361 12.06\% $455.0020262041205620712086210121162131214621612171219222072222223722512266228022932766231823302339234823542358236023612361236110 .84 \%$ $450.00191919361953197019872004202220402057207620942112213121492168218722052224224722612279229723132328234123522358236123612361 \quad 9.63 \%$ $445.00178618051823184218611881190119211941196219832004202620482070209321162140216421882213223722622286231023312349235923612361 \quad 8.41 \%$ $440.00162516451665168517061727174817701792181518381862188719111937196319902015204720772107213921722207224222792315234723612361 \quad 7.19 \%$ $435.0014331453147414951517153915611584160816321656168217081735176217911820 / 851188319171952198920282071211721672223228823562361 \quad$ 5.97\% $430.00120712271248127012921314133713601384140814331459148615131541157 Q 1611633166617001737177618181863191319692034211722482361 \quad 4.75 \%$ 425.009469679871008102910511073109611191143116711921218124512721306 , $329136013911424145914961535157616221671172717901851861 \quad 3.53 \%$ $420.0065167169071073075077179381483685988290693095598010061033106110901120115111821216125012841319134913611361 \quad 2.32 \%$ $415.0032334135837739541343245147149051053055157259361563765968270472775077379581783685186086186101 .10 \%$


 395.00-1275-1267-1258-1249-1241-1233-1225-1217-1209-1202-1194-1187-1181-1175-1169-1163-1158-1154-1150-1147-1144-1142-1140-1140-1139-1139-1139-1139-1139-1139 -3.77\% 390.00-1729-1722-1716-1709-1703-1697-1691-1685-1680-1675-1670-1665-1661-165 -1654-1651-1648-1645-1643-1642-1641-1640-1639-1639-1639-1639-1639-1639-1639-1639-4.99\% 385.00-2196-2191-2187-2182-2178-2173-2169-2166-2162-2159-2155-2153-2150-2148-2146-2144-2143-2141-2141-2140-2139-2139-2139-2139-2139-2139-2139-2139-2139-2139 -6.21\% 380.00-2674-2671-2667-2664-2661-2658-2656-2653-2651-2649-2647-2646-2644-2643-2642-2641-2640-2640-2640-2639-2639-2639-2639-2639-2639-2639-2639-2639-2639-2639 -7.43\% $375.00-3160-3157-3155-3153-3151-3150-3148-3146-3145-3144-3143-3142-3141-3141-3140-3140-3139-3139-3139-3139-3139-3139-3139-3139-3139-3139-3139-3139-3139-3139-8.65 \%$ $370.00-3651-3649-3648-3647-3645-3644-3643-3643-3642-3641-3641-3640-3640-3640-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-3639-9.86 \%$ 365.00 - $4145-4145-4144-4143-4142-4142$ - 141 - 1141 - $140-4140-4140-4140-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-4139-11.08 \%$


## COVERED CALL

## OPTIONS PAYOFF DIAGRAM



## WHAT SHOULD OPTIONS COST?

- Historically: contracts traded individually, over the counter
- How much should you pay? Which factors matter?
- Car insurance policy based on:

| VARIABLE | Sensitivity of value |
| :---: | :---: |
| CARAGE | $?$ |
| CAR VALUE | $?$ |
| YOUR AGE | $?$ |
| YOUR RISK FACTORS | $?$ |
| POLICY COVERAGE | $?$ |

#  

 $500.00234423452344234923502351235323542355235623562357235823582358235923592359235923602360235023602350236023612361236123612361 \quad 21.81 \%$




 $460.00211021232136214921622174218722002712222523372249226122722832204230523152324233223402345235235523592360236123612361236112 .06 \%$ $455.0020262041205620712086210121162131214621612172192200722222372251226622802032306231823302392348235423582360236123612361 \quad 1034 \%$

 $445.0017861805182318421861188119011921194119621983200420262048200020032116214021642138221322372622286231023312349235923612361 \quad 8.41 \%$ $440.00162516451665116851706172717481770179218151888186218871911193719931990201820472072107213921722207242222923315234723612361 \quad 7.19 \%$ $430.0012071227124812701292131413371360138414208143314591486151315411501601163316661700173717618181863191319692034211722482361 \quad 4.75 \%$ $430.0012071227124812701292131413311360138414081433145914861513154115016011633166617001737177618181863191319692034211722482361 \quad 4.75 \%$ $425.0094696798710081029105110731096119114311671192121812451272130013291360139114241459149615351551621671172717901851861 \quad 3.53 \%$ $420.006516716907107307507717938148368598890693095598010061033106110901120115111821216125012841319139913611361 \quad 2.32 \%$ $415.003233413583739541343245147149051053055157259361563765982704727750773795817836851860861861 \quad 1.10 \%$
 $405.00-426-412-399-385-3 / 2-358-345-332-318-305-291-278-265-252-239-226-214-202-191-180-170-162-154-148-143-140-139-139-139-139-1.34 \% /$ $400.00-840-829-818-807-796-785-774-764-753-743-733-723-714-704-695-687-678-671-664-658-652-648 \quad-644-641 \quad 640-639-639-639-639-639-2.56 \%$ $395.00-1227-1267-1258-1249-124-1233-125-1217-120-1202-114-1187-1181-1175-116--1163-1158-115-1150-1147-1144-114-1140-1140-1139-1139-1139-1139-1139-1139-3.77 \%$








Time

# PTIONS VALUE ~ HEAT TRANSFER + RANDOM MOTION 

## BLACK-SCHOLES MODEL

## WHAT DETERMINES OPTIONS PRICE? <br> VARIABLE Sensitivity of option value ("Greeks") <br> STRIKE PRICE <br> STOCK PRICE <br> VOLATILITY <br> INTEREST RATE <br> TIME LEFT <br> Fixed during contract <br> Delta, Gamma <br> Vega <br> Rho

$$
\begin{gathered}
C(S, t)=N\left(d_{1}\right) S-N\left(d_{2}\right) K e^{-r T} \\
d_{1}=\frac{\ln \left(\frac{S}{K}\right)+\left(r+\frac{\sigma^{2}}{2}\right) T}{\sigma \sqrt{T}} \\
d_{2}=d_{1}-\sigma \sqrt{T}
\end{gathered}
$$

| $C(S, t)$ | (call option price) |
| :---: | :--- |
| $N()$ | (cumulative distribution function) |
| $T=\left(T_{1}-t\right)$ | (time left til maturity (in years)) |
| $S$ | (stock price) |
| $K$ | (strike price) |
| $r$ | (risk free rate) |
| $\sigma$ | (volatility) |

## HISTORY

- 1973: Black-Scholes Model published
- 1973: CBOE (first options exchange)
- 1st day: 911 contracts traded
- 1st month: More volume than all OTC
- Today: >44M contracts daily
- 1997: Nobel Prize in Economics



## OPTIONS TRADING: BIG IDEAS

## UNBUNDLE ASSET

$$
\begin{aligned}
& \text { AIRLINE TICKET }= \\
& \text { SEAT }+ \text { FOOD }+ \text { LUGGAGE } \\
&+ \text { VIEW }+\ldots
\end{aligned}
$$

STOCK = 100\% OF
PROFITS/LOSSES FOREVER

OPTIONS = PORTION OF PROFITS/LOSSES FOR SOME TIME

## COMMITMENT = PAID CONTRACT

## GET PAID TO LIST ON EBAY GET PAID TO PREORDER

## SAMPLE COMMITMENTS

WILL BUY AT DISCOUNT WILL SELL AT PROFIT WILL HOLD FOR LONG TERM

## Trading Strategies

INVESTMENT GOAL

BUY POSSIBLE PROFITS

BUY INSURANCE

SELL POSSIBLE PROFITS

DISCOUNTED PREORDER

BUY PROFIT RANGE

SELL PROFIT RANGE

SELL INSURANCE RANGE

Option Strategy
Buy call

Buy put

Hold stock, sell call (covered call)

Have cash, sell put (cash-secured put)

Buy call spread

Sell call spread

Sell put spread

## Trading Strategies

## OPTION STRATEGIES







Filter by market outlook


## EXAMPLE STRATEGY



## Summary



## BONUS: RULE OF 72

Simple Interest


GREEN = DIRECT

Compound Interest (Factory)


PURPLE, ORANGE... = COMPOUND EFFECT

Rule Of 72:
Road Trip To Doubleville

Compound Interest (Factory)


Pct/yr $\rightarrow$ Doubling Time

$$
\begin{aligned}
1 \% & \rightarrow 72 \text { years } \\
2 \% & \rightarrow 36 \text { years } \\
3 \% & \rightarrow 24 \text { years } \\
10 \% & \rightarrow 7.2 \text { years }
\end{aligned}
$$

The time to double is roughly 72 divided by interest rate.

$$
\begin{gathered}
1 * e^{\wedge}\{R T\}=2 \\
R T=\ln (2)=.693 \sim .72 \\
T=.72 / R
\end{gathered}
$$

[change "R=.05" to "R=5"]

$$
T=72 / R
$$

